George Mason University EDCI 552: MATH METHODS FOR THE ELEMENTARY CLASSROOM (3) Fall 2011

Instructor

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By appointment

I. Course Description

This course introduces methods for teaching all children topics in arithmetic, geometry, algebra, probability, and statistics in elementary grades. It focuses on using manipulatives and technologies to explore mathematics and solve problems.

Prerequisite: Admission to the Elementary Education Licensure Program

II. Student Outcomes

This course will enable students to:

A. Know what constitute the essential topics in mathematics of the modern early and intermediate grades school program.

B. Identify and use selected manipulatives and technology such as linking cubes, attribute blocks, geoboards, base-10 blocks, fraction circles, tangrams, calculators, and computers to teach appropriate mathematics content topics in the early and middle grades.

C. Identify and use various instructional strategies and techniques (cooperative and peer group learning, activity centers, laboratories and workshops, teacher-directed presentations, etc.) to teach mathematical content topics appropriate for the early and intermediate grades to all children, including those from non-mainstreamed populations.

D. Identify and use alternative methods for assessing students' work in mathematics in the early and intermediate grades.

E. Solve problems in the mathematical content areas of logic, number theory, geometry, algebra, probability, and statistics appropriate for adaptation to the early and intermediate grades.

F. Know and explain a standards-based mathematics curriculum, the key elements of the National Council of Teachers of Mathematics Principles and Standards for School Mathematics, and the key elements of the Virginia Standards of Learning for Mathematics.

Additionally, this course supports the CEHD Core Values of collaboration, ethical leadership, research-based practice, social justice, and innovation. Statements of these goals are at <u>http://cehd.gmu.edu/values/</u>.

III. Relationship to Program Goals and Professional Organizations Student Outcomes Referenced to Selected National Standards

Course Student	NCTM Principles and	ISTE NETS	ACEI
Outcomes (above)	Standards		
А	S1, S2, S3, S4, S5	SI	1.0
В	S10	SII	3.1
С	P1, P2, P3, P4, P6	SII	1.0, 2.3, 3.1, 3.3, 3.4
D	P5	SIV	4.0
E	S1, S2, S3, S5, S6	SI	2.3
F	S1-10, P1-6	SI	1.0

Key:

NCTM Principles and Standards = National Council of Teachers of Mathematics Principles and Standards for School Mathematics (2000), where P = principles and S = standards.

NETS = International Society for Technology in Education National Education Technology Standards 2000, where S = standard number

ACEI = Association for Childhood Education International Elementary Education Standards

IV. Nature of Course Delivery

In this course we will begin an inquiry into mathematics teaching and learning that will guide you in your first teaching job and give you the tools that will enable you to continue to inquire and learn as part of your work as a teacher. Class sessions will be interactive and will include a variety of hands-on experiences with concrete and virtual manipulatives appropriate for elementary school mathematics. We will explore the teaching of mathematics, investigating both *what* to teach and *how* to teach it. We will explore what it means to do mathematics and what it means to understand mathematics through individual, small group, and large group mathematical problem solving. We will investigate ways to represent understandings of mathematical concepts, communicate reasoning about mathematical ideas, and construct mathematical arguments. We will investigate and read about ways children might represent mathematical concepts, looking at ways to help children build connections and see relationships among mathematical ideas. We will explore characteristics of a classroom environment conducive to mathematical learning by reading and discussing the importance of mathematical tasks, mathematical tools, the roles of teachers and students, and the assessment of mathematical understanding.

V. Required Texts & Readings

Van De Walle, J., Karp, K. S., & Bay-Williams, J. M. (2010). *Elementary and Middle School Mathematics: Teaching Developmentally*. (7th edition) New York: Allyn & Bacon.

A student membership in NCTM is recommended but not required. \$39 per year from http://www.nctm.org/membership/content.aspx?id=7618

VI. Course Requirements and Assignments

Attendance. It is your responsibility to attend all class sessions. You are held accountable for all information from each class session whether you are present or not. Please report your reasons for any absences to the instructor in writing. Tardiness. It is your responsibility to be on time for each class session. Please report your reasons for any tardiness to the instructor in writing.

Assignments. The assignments across the semester are intended to further your understandings of what it means to teach, learn, and assess mathematics in light of current reforms in mathematics education. All assignments are to be turned in to your instructor on time. **Late work will not be accepted for full credit.** If the student makes prior arrangements with the instructor, assignments turned in late will receive a 10% deduction from the grade per late day or any fraction thereof (including weekends and holidays).

Problem Set & Pedagogy Responses (20%) Individual Student Assessment (30%) Lesson Plan Summary Reports (30%) Mathematics Content & Pedagogy Checkpoints (20%)

A. Problem sets, reflections and postings (20%)

Rich, meaningful, problem-based tasks will be assigned for each session. Students are expected to complete these problems before class and incorporate their thinking about strategies used to solve the problems in class discussion. Work on problem sets will be shared in class and on occasion may be collected and evaluated.

Problem Sets: class sessions will consist of working on problem sets and analyzing student work. Problem sets are to be completed before each class session. Students are expected to analyze and reflect solution strategies and come to class prepared to participate in the discussion.

Reflections postings Participants will write reflections on the problems encountered during the course. Participants will complete reflections and may choose the problems/tasks that interest them from those assigned during class. This writing should include three major parts: 1) a description of the problem and an example of the participants' thinking about that problem and multiple strategies; 2) a reflection on changes in the participant's own understanding and thinking with regard to that problem; and 3) related implications for teaching and learning in the K-8 setting. Problem sets and reflections are due on designated due dates (see schedule).

B. Individual Student Assessment (30%) – Performance Based Assessment for the Course In order to plan effective instruction, you will need to know how to assess children's knowledge of mathematical concepts. One way to assess children's thinking is a diagnostic assessment. This assignment has two parts: (1) Design a plan for the assessment, assessing a specific mathematics topic using concrete, pictorial and abstract representations, (2) Conduct the assessment with a child and write a report describing the outcome of the assessment. Based upon feedback from the instructor on your plan, you may make modifications to the final plan and report. (10% PLAN; 20% FINAL **REPORT**)

C. Three Lesson Study Plan Summaries (30%)

You are required to plan, teach, and complete a formal summary for three mathematics lessons during your field placement. The first lesson may be taught in a small group setting, while the other lesson must include the entire class. The format for designing your mathematics lessons is found in your PS Manual. Try to avoid the *overuse* of worksheets. Integrate the use of mathematics tools (manipulatives, calculators, computers) and representations (concrete, pictorial, symbolic) to provide children with an interactive, conceptually-based mathematics experience. The lesson plan summaries are a three-phase process: (1) Design the lesson plan, (2) Teach the lesson in your classroom, and (3) Collect and report evidence of student learning from the lesson in a reflection.

D. Mathematics Content & Pedagogy Assessment (20%)

The Mathematics Content/Pedagogy Assessments will consist primarily of short responses that focus on mathematics content in the elementary grades, with some questions focusing on methodological content. Throughout the semester, brief content-specific assessment will assist you in reviewing important mathematics appropriate for the elementary grades.

<u>Attendance</u>. It is your responsibility to attend all class sessions. You are held accountable for all information from each class session whether you are present or not. Please report your reasons for any absences to the instructor in writing. <u>Tardiness</u>. It is your responsibility to be on time for each class session. Please report your reasons for any tardiness to the instructor in writing.

	LEVEL	OF	PERFORMANCE	
ELEMENT	Distinguished	Proficient	Basic	Unsatisfactory
	(9 – 10 points)	(8 points)	(6 - 7 <i>points</i>)	(1 - 5 points)
Attendance	The student	The student	The student is	The student is
&	attends all	attends	on time,	late for class.
Participation	classes, is on	all classes, is on	prepared for	Absences are
	time, is prepared	time, is prepared	class, and	not
	and follows	and	participates in	documented by
	outlined	follows outlined	group and class	following the
	procedures in	procedures in case	discussions.	procedures
	case of absence.	of	The student	outlined in this
	The student	absence; the	attends all	section of the
	actively	student	classes and if an	syllabus. The
	participates and	makes active	absence occurs,	student is not
	supports the	contributions to	the procedure	prepared for
	members of the	the	outlined in this	class and does
	learning group	learning group and	section of the	not actively
	and the members	class.	syllabus is	participate in
	of the class.	Presentations	followed.	discussions.
	Presentations	demonstrate	Presentations	Presentations are
	demonstrate a deep	sufficient	demonstrate	lacking knowledge
	knowledge of	knowledge of	minimal	of student error
	student error	student error	knowledge of	patterns and
	patterns as well as	patterns as well as	student error	connections to
	implications for	implications for	patterns	teaching.
	teaching.	teaching.		

VII. Evaluation Schema

Determination of the Final Grade: Graduate Grading Scale

А	93%-100%	A-	90%-92%

B+	87%-89%	В	80%-86%
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С	70%-79%	F	Below 70%

The mathematics education courses in GSE's Elementary Education Program integrate pedagogy and mathematics content appropriate for the elementary school grades. For students to earn a grade of A in the course, they must demonstrate excellence in *both* the pedagogical knowledge and the content knowledge of the mathematics appropriate at their level of teaching. Thus, the grading in the course is structured to help evaluate fairly student excellence in both areas. Exam work focuses primarily on ascertaining student excellence in handling mathematics content appropriate for the elementary grades, and represents 50% of students' grades. Pedagogical knowledge is ascertained primarily from readings, assignments and participation in the course, and represents 50% of students' grades. Therefore students who demonstrate excellence in both pedagogical knowledge and content knowledge receive grades of A.

VIII. Course Schedule Course Schedule FALL CLASS SCHEDULE

552- PDS YL

Date	Topic/Learning Experiences	Readings & Assignments due in class
August 30 th	How Do Children Learn Mathematics?	In class Discussion
_	NCTM's Principles & Standards	Van de Walle: Chapters 1 & 2
	Math Autobiography	
September 6th	What is Problem Solving?	Assigned readings:
	A closer look at the MATH SOL	Chapter 3: Problem Solving
	NCTM PROCESS standards	Chapter 4: Planning Problem Based
September 13 th	Planning for Mathematics Instruction	Chapter 8: Early numbers
	Number Sense, Counting, Patterns & Place	Chapter 5 Assessment
	Value/Basic Facts & Whole Number Operations	
C 1 20st		
September 20 ^{se}	Assessment – Conducting a Diagnostic	Chapter 9: Meanings for Operation
	Interview Numbers and operations	Chapter 6: Equity
	In Class Discussion of Lesson Plan #1	*Losson Dian #1 DUE today
	*Lesson Plan #1 DUE	Lesson Flan #1 DOE today
September 27 th	COMMUNICATION: Promoting Math talk	Assigned readings *
September 27	Mathematics Content & Pedagogy	Chapter 11 Place value
	Assessment	Chapter 12 whole number
	Assessment	
October 4th	Algebraic Thinking	Chapter 13 Computation w/ Whole Numbers
		Chapter 14 Algebraic Thinking
		Individual Student Assessment PLAN DUE
October 11 th	No meeting	
October 17 th	Fraction	Chapter 15 Fractions
October 25 th	Fraction Concepts and Computation	Assigned readings*
	MULTIPLE REPRESENTATIONS	Van de Walle:
		Chapter 16 Fractions Operations
November 1 st	Rational number concepts	Assigned readings *
	*Lesson Plan #2 DUE (Share out)	Chapter 17 Decimals percent
th		*Lesson Plan #2 DUE
November 8 th	Proportional reasoning	Assigned readings
	Mathematics Content & Pedagogy	Chapter 18 Proportional reasoning
4	Assessment	
November 15 th	Measurement	Assigned readings
		Chapter19 Measurement
10.11		
12-November	Geometry	Chapter 20 Geometry
22	*Lesson Plan #3 DUE (share out in class)	
November 20 th	Data Analysis	Chapter 21 Data Analysis
		Lesson Plan #3 Due
December 6 th	Probability Experiments	Chapter 22 Probability
	Mathematics Content & Pedagogy	
	Assessment	
December 13 th	Individual Student Assessment Final REPORT	Individual Student Assessment DUE
	DUE	Reading from TCM
December 20th	Panel Discussion	Math Philosophy Revised
		Reading from TCM

IX. University Policies

GSE Syllabus Statement of Expectations

A. The Graduate School of Education (GSE) expects that all students abide by the following: Students must adhere to the guidelines of the George Mason University Honor Code [See http://academicintegrity.gmu.edu/honorcode/].

B. Students with disabilities who seek accommodations in a course must be registered with the George Mason University Office of Disability Services (ODS) and inform their instructor, in writing, at the beginning of the semester [See <u>http://ods.gmu.edu/</u>].

C. Students must follow the university policy for Responsible Use of Computing [See <u>http://universitypolicy.gmu.edu/1301gen.html</u>].

D. Students are responsible for the content of university communications sent to their George Mason University email account and are required to activate their account and check it regularly. All communication from the university, college, school, and program will be sent to students solely through their Mason email account.

E. Students must follow the university policy stating that all sound emitting devices shall be turned off during class unless otherwise authorized by the instructor.

F. Students are expected to exhibit professional behaviors and dispositions at all times.

X. CEHD Statement of Campus Resources:

A. The George Mason University Counseling and Psychological Services (CAPS) staff consists of professional counseling and clinical psychologists, social workers, and counselors who offer a wide range of services (e.g., individual and group counseling, workshops and outreach programs) to enhance students' personal experience and academic performance [See <u>http://caps.gmu.edu/</u>].

B The George Mason University Writing Center staff provides a variety of resources and services (e.g., tutoring, workshops, writing guides, handbooks) intended to support students as they work to construct and share knowledge through writing [See <u>http://writingcenter.gmu.edu/</u>].

For additional information on the College of Education and Human Development, Graduate School of Education, please visit our website [See <u>http://gse.gmu.edu/</u>].

Approved March 2004, Revised August 2011

The College of Education & Human Development is committed to the following five values: collaboration, ethical leadership, innovation, research-based practice, and social justice . Students are expected to adhere to these principles. <u>http://cehd.gmu.edu/values/</u>

Lesson Plan GRADING REQUIREMENTS

GENERAL REQUIREMENTS:

* The lesson plans must be handed in on time. (If the lesson is not handed in on time, subtract 10% from the total score on the report per late day.)

* Your Clinical Teacher may choose to write a formal observation of one of your lessons, or you may ask him/her for feedback on your lesson.

* You must integrate manipulatives, literature, and/or technology into your lessons.

The LESSON

Objectives

The objectives clearly state what students will do during the lesson.

The objectives clearly state the mathematics content/essential understandings of the lesson.

The objectives are tied to state/national standards.

The objectives are tied to the assessment; this information is provided in the assessment section of the report.

Materials

A list of materials used during the lesson is provided.

A copy of the materials is included with the lesson.

A variety of materials are used in each lesson (manipulatives, technology, etc.).

The lesson integrates the use of mathematics tools (manipulatives, calculators, computers) and/or representations (concrete, pictorial, symbolic).

The teacher creates materials for the lesson.

Appropriate materials are selected for the concepts being taught.

The lessons do not overuse worksheets.

Procedure

The lesson is substantive in length, breadth, and depth.

Any questions and mathematics content the teacher uses during the lesson are included in the procedures.

The procedures thoroughly and completely outline what the teacher will do during the lesson; How did you present the lesson?

The procedures are in a bulleted list, approximately 1-2 pages in length.

The procedures provide enough detail to allow another person to teach the lesson.

* LINK- The procedures include an introduction for activating prior knowledge.

* ENGAGE AND EDUCATE- The procedures show that students are engaged in <u>doing</u> mathematics during the lesson.

* ACTIVE LEARNING- The procedures thoroughly and completely outline what the students will do during the lesson. Estimated times for each phase are provided in parentheses.

*REFLECT-The procedures include a plan for closing the lesson and checking for understanding.

* NOW and THEN- Connecting to other concepts

Assessment / Work Samples

The assessment used during the lesson is described in approximately $\frac{1}{2}$ -1 pages.

The description of the assessment is clear enough that another person could conduct the assessment; What was the assignment?

The assessment describes what the teacher does to assess the students.

The assessment describes in detail what the students do to demonstrate their understanding of the concept.

An example of the assessment conducted during the lesson is attached to provide documentation of what students did during the lesson (i.e., written work, drawings, worksheets, photographs, checklists, anecdotal records).

The objectives are tied to the assessment; this information is provided in the assessment section of the report.

Differentiation Gearing up and gearing down

A list of adaptations for individual students is included.

Specific information must be provided on individual students in the class and the accommodations made for those children. (General comments are **not** appropriate for this requirement.)

Reflection

The reflection is 1 -2 pages in length for any lesson you teach in the classroom.

A portion of the reflection describes the mathematics teaching and learning that occurred during the lesson and how it related to the lesson plan prepared ahead of time.

A portion of the reflection discusses those elements of the lesson that went well and those that did not.

A portion of the reflection discusses at least three changes or improvements that you would make to the lesson if you were teaching it again.

A portion of the reflection identifies one important idea you learned about teaching and learning mathematics from the lesson. (Ideas that focus on behavior management strategies are **not** acceptable for this requirement.)

A portion of the reflection identifies one important teaching skill you plan to work on the next time you teach a mathematics lesson.

Critorio	Expectations	Points Awarded/Points
Criteria	Expectations	Possible
	1. The objectives clearly state what students will do during the lesson.	
Objectives	2. The objectives clearly state the mathematics content/essential understandings	(10)
	of the lesson and the objectives are tied to state/national standards.	
	1. A list of materials used during the lesson is provided.	
Materials	2. Copies of any handouts or worksheets used during the lesson are included.	
	5. The resson integrates the use of mathematics tools (manipulatives,	(5)
	Appropriate materials are selected for the concepts being taught	(3)
	 The lesson does not <i>overuse</i> worksheets 	
	1. The lesson is substantive in length, breadth, and depth.	
Procedure	2. The procedures thoroughly and completely outline what the teacher will do	
	during the lesson. How did you present the lesson?	
	3. The procedures thoroughly and completely outline what the students will do	(40)
	during the lesson.(Anticipate students' responses)	、 /
	4. The procedures show that students are engaged in <u>doing</u> mathematics.	
	5. Estimated times for each phase are provided in parentheses.	
	6. Any questions or mathematics content the teacher uses during the lesson are	
	included.	
	7. The procedures include an introduction for activating prior knowledge and a plan for closing the lesson.	
	1. A list of adaptations for individual students is included.	
Differentiation	2. Specific information must be provided on individual students in the class and	
	the accommodations made for those children. (General comments are not	
	appropriate for this requirement.)	(10)
	1. The assessment is tied to the lesson objectives.	
Assessment	2. The assessment is described in enough detail that another person could	
	conduct the assessment.	
	3. The assessment describes what the teacher does to assess the students.	(10)
	4. The assessment describes anticipated student responses. What will students do to demonstrate their understanding of the mathematics? What students	
	misconceptions do you predict?	
	1 An example of the assessment conducted during the lesson is attached to	
Work Samples	provide documentation of what students did during the lesson (i.e., written	
() of it Sumples	work, drawings, worksheets, photographs, checklists, anecdotal records).	
	2. Brief analysis of the outcome of the assessment.	(5)
	1. The reflection describes the mathematics teaching and learning that occurred	
Reflection	during the lesson and how it related to the lesson plan prepared ahead of	
	time.	
	2. The reflection discusses those elements of the lesson that went well and those	(20)
	that did not.	
	5. The reflection discusses at least three changes or improvements that you would make to the losson if you were teaching it again	
	4 The reflection identifies one important idea you learned about teaching and	
	learning mathematics as well as one important teaching skill you plan to	
	work on the next time you teach a mathematics lesson. (Ideas that focus on	
	behavior management strategies are not acceptable for this requirement.)	
	Total Points	(100)

SCORING RUBRIC FOR LESSON PLANS

Individualized Student Assessment Guidelines (Performance Based Assessment for the Course)

PLAN

Student Assessment PLAN

The Child:

Describe the child you plan to assess. Include information you gathered about the child (grade level, age, gender, race, and academic ability level). What do you know about the child's level of understanding about the topic *before* the assessment?

The Mathematics Concept:

Select one specific mathematics concept to assess during the assessment. Examples of concepts might include patterns, sorting, addition of whole numbers, division of fractions, finding averages, percent, geometric shapes, or length measurement. Tell why this concept is appropriate for this child at this particular grade level.

Different Forms of Representation:

During the assessment, assess the child using three different forms of representation. Identify the three different forms of representation you will use during the assessment with at least one example in each form. *Concrete* representations include manipulatives, measuring tools, or other objects the child can manipulate during the assessment. *Pictorial* representations include drawings, diagrams, charts, or graphs that are drawn by the child or are provided for the child to read and interpret. *Symbolic* representations include numbers or letters the child writes or interprets to demonstrate understanding of a task.

Tasks & Questions:

Design tasks and questions that use three different forms of representation (concrete, pictorial, abstract symbols) to diagnose the child's understanding of ONE basic concept. Go beyond the basic level of determining the child's factual knowledge of the concept by asking questions that determine how much the child understands about the concept. For example, suppose you are assessing the concept of ADDITION. (1) Create several tasks where the child uses concrete manipulatives to demonstrate her understanding of addition; ask questions about the child's understanding of the addition tasks with manipulatives. (2) Create several tasks where the child is asked to create or interpret drawings to demonstrate her understanding of addition; ask questions about the child's understanding of these tasks with pictorial models; (3) Create several tasks where the child uses abstract symbols (and letters) to demonstrate her understanding of addition; ask guestions about the child's understanding of these addition tasks using the symbols.

The plan should be typed.

Individual Student Assessment Guidelines (Performance Based Assessment for the Course) REPORT

Student Work Samples:

Collect and document three different forms of representation (concrete, pictorial, abstract symbols) during the assessment to elicit the child's level of understanding. The report must include samples of the child's computations, writings and drawings, as well as a description of how the child used concrete objects during the assessment or photographs of the child's work.

Question & Response Assessment Excerpts:

Type key excerpts from the assessment. Type only those questions and responses that pertain to mathematics. Be sure to include your questions and the child's responses. Indicate what you said and what the child said by using T for you (the teacher) and C for the child.

Questioning Competence:

The questions and follow-up questions that you use during the assessment will be evaluated. You will be evaluated on the *quality* and the *types* of follow-up questions you use during your interaction with the child. Your textbooks and readings provide direction on the types of questions that are appropriate in an assessment and that go beyond factual information to deeper understanding.

Evaluation of Child's Mathematical Knowledge:

Write an evaluation of the child's mathematical knowledge in the content area. Use evidence from the assessment to support your conclusions. Use your textbook to help you describe the specific types of behaviors and verbalizations you observed using specific mathematical terms. For example, if you conclude that the student has an understanding of addition of fractions with like denominators, you should

base this on evidence that you present that shows the child was able to represent $\frac{3}{5}$ and $\frac{4}{5}$ with fraction

pieces (concrete), and/or the child used a drawing to find the sum (pictorial), and/or the child computed the answer with symbols (abstract). Give specific examples of the child's responses to support your statements.

Instructional Plan:

Develop a suggested instructional plan for the child. Your assessment of the child's thinking should give you some information for planning instruction. Your suggestions should be based on what you learned about the child during the assessment. Many general suggestions can be valuable for children. However, your recommendations should relate to specifics. For example, if you assessed basic division concepts and you suggest that the instructional plan for the child should include more manipulatives, that would be an important teaching strategy, but it would be too general. You should be more specific about why and how manipulatives might be used. Example: "The student had difficulty making 3 equal groups from a set of 21 chips; therefore, the student should be given more experiences with grouping and partitioning manipulatives in sets of 15 to 30 to develop both the measurement and partitive concepts of division."

Reflection of the Assessment Process:

Comment on the assessment process. How long did the assessment last? What did you learn about assessment techniques? What did you learn about your ability to create mathematics questions and tasks for this concept? If you were to conduct the assessment with another child, would there be any changes in your questions, either the order or the level of difficulty, or the materials you had available for the child to use? Why or why not? What have you learned about how children learn mathematics from this assessment? How might a classroom teacher use the diagnostic mathematics assessment to assess children?

The report should be typed.

RUBRIC FOR ASSESSMENT REPORT

Criteria	Exceeds Requirements (A)	Meets Requirements (A - B+ B)	Needs Improvement (C)	Inc	
Chicha	Exceeds requirements (A)	frees requirements (A-,D-,D)	recus improvement (C)	inc.	Weight
Is the required information present about the <u>child</u> assessed?	5 In addition to the required information, the Report includes information about the child's performance in other academic, social, or behavioral areas. Cite references.	4 3 2 The Report includes the child's grade level, age, gender, race, academic ability level, and the child's level of understanding about the mathematics concept.	l One or more of the required descriptive items about the child is missing.	0	x .05 =
Has the teacher selected one specific mathematics <u>concept</u> and assessed the concept using three different <u>forms of</u> <u>representation</u> (concrete, pictorial, abstract)?	⁵ Information on age-appropriate variations of the mathematics concept was gathered in preparation for the assessment. One math concept is clearly described and mathematically accurate. Three different forms of representation, with different examples in each form, are designed for use in interesting and creative ways. Connections are made among representational forms. Cite references.	4 3 2 One age-appropriate mathematics concept is selected, mathematically accurate, and clearly described. Three different forms of representation are described and used appropriately to assess the mathematics concept. Different examples may be used within each representational form.	l One or more mathematics concepts are selected. They may not be age-appropriate. The Report is missing one or more forms of representation.	0	x .10 =
Do the <u>tasks and</u> <u>questions</u> match the specific mathematics concept being assessed? Is there variety in the tasks and questions used for each of the three different forms of representation?	5 In addition to the tasks/questions being aligned with the math concept, there are questions that differentiate and provide extensions for different levels of student performance. In addition to the variety of tasks/questions for each of the three forms of representation, tasks that show creativity and will be motivating for a child are included. Cite references.	4 3 2 The tasks and questions designed for the assessment are aligned with the mathematics concept being assessed. There are a variety of tasks and questions for each of the three forms of representation.	1 The tasks and questions designed for the assessment are not clearly aligned with the mathematics concept being assessed. The Report is missing tasks/questions that address one or more of the forms of representation.	0	x .15 =
Are the child's <u>work</u> <u>samples</u> included with three different forms of representation present in the work samples?	5 In addition to the variety of work samples from the child showing examples in each of the three forms of representation, a creative way of providing an explanatory overview of the child's work is included.	4 3 2 There are a variety of work samples from the child included showing examples in each of the three forms of representation. (concrete, pictorial, abstract)	1 There is only one work sample in each of the three forms of representation or work samples from one form of representation are missing.	0	x .10 =
Is the required question and response assessment <u>excerpts</u> present?	5 The Report includes key excerpts from the mathematics assessment that includes descriptive information on both the behaviors and the actual verbalizations that occurred during the assessment.	4 3 2 The Report includes excerpts of the mathematics assessment using the teacher and the child's actual verbalizations from the assessment (T for teacher; C for child).	1 The Report includes excerpts of the mathematics assessment, but some parts of the assessment conversation are limited.	0	x .15 =
Do the initial and follow- up <u>questions</u> used by the teacher demonstrate variety and higher levels of questioning? Are specific follow-up questions used appropriately?	5 The transcript shows that during the assessment, the teacher used a variety of questions to encourage the child to express his/her thinking, used many higher-level questions to encourage deeper thinking and responses from the child, and used specific follow-up questions to probe for understanding.	4 3 2 The transcript shows that during the assessment, the teacher used a variety of higher-level questions to encourage deeper thinking and appropriate follow-up questions to probe for understanding.	1 The transcript shows that during the assessment, the teacher used very few probing and follow-up questions when a specific follow-up question would have been appropriate.	0	x .10 =
Does the <u>evaluation</u> accurately represent the child's current level of understanding on this concept using supporting evidence and work samples from the assessment?	5 The evaluation provides an accurate and detailed description of the child's current level of understanding on the concept. Many different and specific examples from the assessment are given, including the child's quotations, student work, and information from other sources on math development, to provide supporting evidence for the evaluation of the child.	4 3 2 The evaluation provides an accurate description of the child's current level of understanding on the mathematics concept. Different examples from the assessment are given, including the child's quotations and student work, to provide supporting evidence for the evaluation.	1 The evaluation provides a minimal description of the child's understanding on the mathematics concept. A few examples from the assessment are given, but there is not enough information to provide supporting evidence for the evaluation.	0	x .15 =
Does the <u>instructional</u> <u>plan</u> prescribe developmentally appropriate next steps for instruction and take into account the child's current level of understanding on this concept?	5 The plan is a creative, detailed description of developmentally appropriate next steps for instruction taking into account the child's current level of understanding. The plan identifies many specific examples of activities and tasks that would further enhance this child's knowledge of this concept. Information from other sources on math development and child development was used. Cite references.	4 3 2 The instructional plan describes developmentally appropriate next steps for instruction. The plan identifies several specific examples of tasks that would be appropriate to further enhance this child's knowledge on this concept. The plan describes these tasks in relation to the child's current level of understanding.	1 The plan describes some next steps for instruction that may not be developmentally appropriate. The plan gives general (rather than specific) examples of activities and tasks for the child. The tasks may not be appropriate either for the child or the development of the math.	0	x .10 =
Is there an appropriate reflection and evaluation of the assessment process?	5 In addition to the required information, the Report includes a detailed analysis, self- reflection, and self-evaluation of the assessment process.	4 3 2 The Report includes a reflection and evaluation on the assessment process including the required elements.	The Report does not include one or more of the required elements for the reflection.	0	x .10 =
TOTAL SCORE					
A	5.0 - 4.5				
A- B+	4.47 - 3.3 3.49 - 2.5				
В	2.49 - 2.0				
C	1.99 – 1.0				