

*George Mason University College
of Education and Human
Development*
Secondary Education Program
**EDCI 572: Teaching Mathematics in the
Secondary School**
CRN: 73310
Section #:001



Promoting Learning  Development Across the Lifespan

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Students learn mathematics through the experiences that teachers provide. Thus, students' understanding of mathematics, their ability to use it to solve problems, and their confidence in, and disposition toward, mathematics are all shaped by the teaching they encounter in school.

Teaching mathematics well is a complex endeavor, and there are no easy recipes for helping all students learn or for helping all teachers become effective. Nevertheless, much is known about effective mathematics teaching, and this knowledge should guide professional judgment and activity.

(NCTM, 2000, pp. 16-17)

Purpose of the Course

As a future secondary mathematics teacher, you have the opportunity to shape the future. You can play an important role in the development of adolescents and have an influence on the way in which they come to understand the world in which they live. You can help students to develop strong understandings of mathematics and its uses, understandings that are foundational for work beyond high school. Further, you can shape their dispositions toward learning mathematics. You have chosen an amazing and rewarding career path!

In this course, you will come to develop knowledge, skills, and understandings that will be useful to you in your work as a secondary mathematics teacher. Though there are no “easy recipes” for helping students learn mathematics, research has identified *characteristics* of effective mathematics teaching. Throughout the semester, we will explore these characteristics and ways in which you can incorporate them into your teaching. You will learn how to be reflective about your work and that of other teachers so that you can continue to draw on and build upon the knowledge and understandings you gain in this course throughout your career as a secondary mathematics teacher who is equipped to help *all* children thrive in secondary mathematics classrooms.

Course Description as provided in the Course Catalog

This course emphasizes developing different styles of teaching and covers curricula, current issues, and research literature in secondary school mathematics. School-based field experience required. This course is for students who have already taken or are concurrently taking EDUC 522.

Objectives

Success in this course is measured by the degree to which you are able to:

- demonstrate an understanding of the ways in which students develop strong, usable understandings of secondary mathematics content (NCTM SPA Standards 7, 8; CEHD Core Value of Research-Based Practice)
- analyze instruction and instructional materials for their potential to promote student learning of secondary mathematics content in diverse settings (NCTM SPA Standards 1, 2, 3, 4, 5; CEHD Core Value of Research-Based Practice and Social Justice)
- design tasks, including those that rely on technology, that foster the development of deep understanding of secondary mathematics concepts (NCTM SPA Standard 6; NCTM SPA Indicators 7.4 and 8.8; CEHD Core Values of Research-Based Practice and Innovation)
- justify instructional decisions by reference to research findings, national standards, and learning theory (NCTM SPA Indicators 7.4; 8.1, 8.4, 8.6, and 8.7; CEHD Core Values of Collaboration and Research- Based Practice)
- demonstrate the dispositions appropriate to work as a secondary mathematics teacher (NCTM SPA Standard 7; CEHD Professional Dispositions)
- continue to develop your own knowledge of mathematics and problem solving ability as you explore
- mathematics from the perspective of a teacher and student (NCTM SPA Standard 1; NCTM SPA Indicators 10.4, 10.5, 11.4, 13.2, 14.6; CEHD Core Value of Innovation)
- analyze different perspectives on mathematics teaching and learning - graduate students only (NCTM SPA Indicator 8.6; CEHD Core Value of Research-Based Practice)

Plan for the Course

We will address the guiding questions and objectives as we progress through the course, which is organized into four sections:

- I. The Nature of Mathematics and Current Thinking in Mathematics Teaching and Learning**
In this part of the course we will explore the nature of doing and understanding mathematics. You will become familiar with the reform movement in mathematics education and the factors that catalyzed that movement. You will also become familiar with the resulting recommendations for teaching and learning offered by the National Council for Teachers of Mathematics (NCTM).
- II. The Learning/Classroom Environment**
In this part of the course, you will become familiar with various characteristics of effective mathematics teaching. You will explore ways of using questioning, group activity, and well-designed mathematics tasks to promote the development of strong understandings of secondary mathematics concepts. And, you will examine curricular resources and standards documents in consideration of they made be used to design instruction.
- III. Planning Instruction**
In this part of the course you will apply the knowledge gained in the previous two sections of the course to instructional design. Throughout this section, you will learn how mathematics content can be organized into a series of lessons.
- IV. Technology**
In this part of the course you will apply the knowledge gained in the previous three sections of the course to implementing technology into lessons. Throughout this section, you will learn how technology may aid in the conceptual understanding of mathematics content.

Textbooks and Materials

Daily access to the following materials is required:

Brahier, D.J. (2012). *Teaching secondary and middle school mathematics* (4th edition). Boston: Pearson Education Inc.

Donovan, M. S., & Bransford, J. D. (2005). *How students learn: Mathematics in the classroom*. Washington, D.C.: The National Academies Press. We will look at excerpts from this text, which can be retrieved from the following website: http://www.nap.edu/catalog.php?record_id=11101

Kilpatrick, J., Swafford, J., & Findell, B. (2001). *Adding it up: Helping children learn mathematics*. Washington, D.C.: The National Academies Press. We will look at excerpts from this text, which can be retrieved from the following website: http://www.nap.edu/catalog.php?record_id=9822

National Council of Teachers of Mathematics (2000). *Principles and standards for school mathematics*. Reston, VA: Author. Excerpts can be found on-line at <http://standards.nctm.org/>

National Governors Association Center for Best Practices, Council of Chief State School Officers. (2010). *Common Core State Standards Mathematics*. National Governors Association Center for Best Practices, Council of Chief State School Officers, Washington D.C. The standards can be retrieved from: <http://www.corestandards.org/Math>

Virginia Standards of Learning available at <http://www.pen.k12.va.us/VDOE/Superintendent/Sols/home.shtml>

Recommended:

NCTM Student Membership. Provides access to (1) Online subscription to *Teaching Mathematics* in the Middle School (for the middle grades), *Mathematics Teacher* (for the high school grades), or other school journals, (2) Online NCTM 2000 *Principles and Standards for School Mathematics*; and (3) access to online articles; available from the National Council of Teachers of Mathematics, 1906 Association Drive, Reston, VA 22091; 703-620-9840; www.nctm.org website.

Course Expectations/Assignments

The following assignments will help you (and me) to gauge your development throughout the course:

Assessment	Due Date	Percentage of Graduate Grade:
Participation and Preparation (includes weekly design experience/example assignments and readings)		20%
Mathematics Autobiography		10%
Procedural/Conceptual Assignment		10%
Field Work Assignments		10%
<i>Collection of Activities: Analysis and Critique</i>		10%
4 Lesson Design Plans		40%

Participation and Preparation

The participation of each class member is vitally important. If you do not come prepared to discuss the readings, to share your work on a given assignment, and to participate in the activities of the day the entire class will suffer. You **must** commit to be coming to every class on time, being prepared for the evening's activities, and being ready to participate. You can expect that, in addition to work on the larger projects outlined below, there will be weekly readings and assignments that will fall into this category. If, however, there is an emergency and you cannot make it to class, you **must email me ahead of time** and submit all assignments electronically before the end of class.

Due Dates, Late Assignments, and Revised Assignments

- *Due Dates:* All assignments are due by 11:59pm of the date assigned.
- *Late Assignments:* If an assignment is not uploaded by 11:59pm of the date assigned, and you have not contacted me to receive an extension, then the assignment will be considered late. All late assignments will receive a *one-letter grade penalty*. If you know that you are going to have an issue with completing an assignment on time, please **notify me ahead of time** to avoid this late grade penalty.
- *Revised Assignments:* When students earn less than 80% on an assignment, I often offer them the opportunity to revise and resubmit. As long as students meet the guidelines for resubmission, students may earn up to 75% of the missed points on the assignment. Please keep in mind that it requires additional work to grade revised assignments, so they will require additional time to re-grade.

Major Assignment Descriptions

Mathematics Autobiography

John Graham's famous quote states, "We teach who we are." Contemporary research in mathematics education finds this to be especially true for secondary mathematics teachers. It is important to examine our own assumptions about teaching and learning mathematics as result of our leaning experiences. In this activity, you will spend some time reflecting on your personal experiences as a mathematics learner. You will use your responses as part of an in-class activity as well as a culminating activity at the end of the course.

Procedural/Conceptual Assignment

Individuals can understand mathematics in different ways. In order to demonstrate proficiency in mathematics, one needs, among other things, both procedural knowledge and conceptual understanding of mathematics. Teachers need to design lessons that develop both. A first step is outlining what those terms mean with respect to the concept a teacher is about to teach. In this assignment, you will have the opportunity to analyze a mathematical concept and to explain what it means to have procedural knowledge and conceptual understanding of that concept.

Field Work Assignments

One of the most valuable pieces of pre-service teacher training is the opportunity to do field work. You will complete 15 hours of field work and keep a log of these hours for submission at the end of the semester.

Throughout the semester, you will be required to complete observation assignments during your field work. These assignments provide you with opportunities to reflect upon the practice of teaching after having watched instances of teaching in real world settings.

Collection of Activities: Analysis and Critique (Graduate Students, Only)

This assignment will give you the opportunity to build your repertoire of teaching "tools." You will choose a mathematics topic covered in middle or high school mathematics curricula and search practitioner journals for ideas to teach that topic. You will then summarize and critique those ideas and consider ways that you might use them (possibly in modified form) in your future work as a teacher. You will then share these ideas with your classmates so that everyone will have a collection of teaching ideas to take with them.

Lesson Plan Assignments and Design Conferences

Throughout the semester, you will explore many issues related to the teaching and learning of mathematics. In 4 instances, you will have the opportunity to use the knowledge, skills, and understandings you have gained in the creation of a series of 4 lesson plans. Within these lessons, you will design lessons that pay attention to the use of technology, the development of student understanding of mathematics content, various standards documents, and problem-based instruction. A template will be provided in class to help you outline your lesson. After the first and third lesson plan submission, the instructor will give you feedback on your lessons in design conferences scheduled outside of class. In addition, you will present your lesson to your peers so that the entire class can begin to create a collection of teaching ideas for various content areas within secondary mathematics. You must meet minimum standard on this, or you will be asked to resubmit.

Communication

You must have a GMU email address (and you must check it often as I will **only** communicate via this medium), you must be able to access Bb (<https://courses.gmu.edu/>), and you must be able to use the library's collection of e-journals. The best way to contact me is through email, rather than phone.

Evaluation

Final course grades will be assigned based upon weighted percentages as indicated by the Course Expectations.

A	93-100%
A-	90-92%
B+	88-89%
B	80-87%
C	70-79%
F	Below 70%

TaskStream Requirements

Every student registered for any Secondary Education course with a required performance-based assessment is required to submit this assessment to TaskStream (regardless of whether a course is an elective, a onetime course or part of an undergraduate minor). Evaluation of the performance-based assessment by the course instructor will also be completed in TaskStream. Failure to submit the assessment to TaskStream will result in the course instructor reporting the course grade as Incomplete (IN). Unless the IN grade is changed upon completion of the required TaskStream submission, the IN will convert to an F nine weeks into the following semester.

GMU Policies and Campus Resources

- Students must adhere to the guidelines of the George Mason University Honor Code [See <http://oai.gmu.edu/honor-code/>].
- Students must follow the university policy for Responsible Use of Computing [See <http://universitypolicy.gmu.edu/policies/responsible-use-of-computing/>].
- Students are responsible for the content of university communications sent to their George Mason University email account and are required to activate their account and check it regularly. All communication from the university, college, school, and program will be sent to students solely through their Mason email account.
- The George Mason University Counseling and Psychological Services (CAPS) staff consists of professional counseling and clinical psychologists, social workers, and counselors who offer a wide range of services (e.g., individual and group counseling, workshops and outreach programs) to enhance students' personal experience and academic performance [See <http://caps.gmu.edu/>].
- Students with disabilities who seek accommodations in a course must be registered with the George Mason University Office of Disability Services (ODS) and inform their instructor, in writing, at the beginning of the semester [See <http://ods.gmu.edu/>].
- Students must follow the university policy stating that all sound emitting devices shall be turned off during class unless otherwise authorized by the instructor.
- The George Mason University Writing Center staff provides a variety of resources and services (e.g., tutoring, workshops, writing guides, handbooks) intended to support students as they work to construct and share knowledge through writing [See <http://writingcenter.gmu.edu/>].

Professional Dispositions

- Students are expected to exhibit professional behaviors and dispositions at all times.

College Expectations

The College expects students to exhibit the following Professional Dispositions:

Commitment to the profession

Promoting exemplary practice
Excellence in teaching and learning
Advancing the profession
Engagement in partnerships

Commitment to honoring professional ethical standards

Fairness
Honesty
Integrity
Trustworthiness
Confidentiality
Respect for colleagues and students

Commitment to key elements of professional practice

Belief that all individuals have the potential for growth and learning
Persistence in helping individuals succeed
High standards
Safe and supportive learning environments
Systematic planning
Intrinsic motivation
Reciprocal, active learning
Continuous, integrated assessment
Critical thinking
Thoughtful, responsive listening
Active, supportive interactions
Technology-supported learning
Research-based practice
Respect for diverse talents, abilities, and perspectives
Authentic and relevant learning

Commitment to being a member of a learning community

Professional dialogue
Self-improvement
Collective improvement
Reflective practice
Responsibility
Flexibility
Collaboration
Continuous, lifelong learning

Commitment to democratic values and social justice

Understanding systemic issues that prevent full participation
Awareness of practices that sustain unequal treatment or unequal voice
Advocate for practices that promote equity and access
Respects the opinion and dignity of others
Sensitive to community and cultural norms
Appreciates and integrates multiple perspectives

Schedule

The dates are subject to change dependent on the progress of the course. I will not move due dates for major assignments to an earlier date, only a later date if necessary. Additional smaller assignments and readings may be made each week. Additionally, at times different students will read different readings and share their understandings with the class. All readings noted as “selected readings” will be available on BlackBoard the week before they are to be read for class.

Date	Topic	Readings	Assignment Due
Aug 26	The Nature of Mathematics and the Reform Movement in Mathematics Education <ul style="list-style-type: none"> • The State of Mathematics Education • Trends in Mathematics Education • Creating a Vision for Your Mathematics Teaching • Why Teach Mathematics? 	Brahier: Chapters 1 and 2	
Sept 2	Mathematical Proficiency <ul style="list-style-type: none"> • Examining Our Mathematical Experiences • What does it mean to be “mathematically proficient”? • Student status and motivation as it relates to proficiency 	Donovan & Bransford: pp. 217-224; 231-236; 236-240	Mathematics Autobiography Due (Submit by email)
Sept 9	Learning Theory and Implications for Instruction <ul style="list-style-type: none"> • Constructivist & sociocultural perspectives on learning mathematics • Conceptual vs. procedural understanding • What does it mean to create rich, student-centered tasks? 	Brahier Ch. 3: pp. 47-50; 57-66 (3 rd ed.) pp. 48-50; 56-66 (4 th ed.) Kilpatrick et al: pp.115-124; 131-133	
Sept 16	Learning Theory and Implications for Instruction <ul style="list-style-type: none"> • Using manipulatives to support learning • Differentiating Learning for All Students Lesson Experience #1	Brahier rest of Chapter 3; pp. 176-180 (3 rd & 4 th ed.) Selected reading – see course site	

Sept 23	Establishing a Learning Environment Conducive to Student Engagement <ul style="list-style-type: none"> • Classroom set-up • Role of Discourse • Effective Questioning • Cooperative Learning Lesson Experience #2	Brahier: rest of Chapter 7 Donovan & Bransford: pp. 225-231; 241-242 Selected reading – see course site	
Sept 30	Instructional Design and Learning Objectives <ul style="list-style-type: none"> • NCTM Curricular Standards • State- and Local-level Objectives • Common Core Standards • Implementing a Course of Study <ul style="list-style-type: none"> ○ Goals and Objectives ○ Role of Textbooks ○ Alternative Sources Lesson Experience #3	Brahier: Chap 4 and 5	Procedural/Conceptual Assignment Due (Upload to <u>TaskStream</u>)
Oct 7	Planning for Instruction (Lesson Planning) <ul style="list-style-type: none"> • Components of Lesson Plans • Role of reflection Lesson Experience #4	Brahier: pp. 142- 166 (3 rd ed) pp. 141-166 (4 th ed.)	
Oct 14	No Class (Spring Break)		
Oct 21	Planning for Instruction (Lesson Planning) Continued <ul style="list-style-type: none"> • Lesson Plan Components (continued) • Launching Lessons • Effectively Summarizing Lessons 	Selected readings – see course site	At least 7 hours of field work completed with accompanying documents Lesson Plan #1 Due
Oct 28	Effective Use of Technology Group 1 Presents Lesson Plans	Brahier: pp. 180-182 (3 rd ed.) pp. 181-183 (4 th ed)	Scheduled Design Conference
Nov 4	Effective Use of Technology (cont.)	Selected readings - See course syllabus	Lesson Plan #2 Due
Nov 11	Considerations for Teaching Algebra <ul style="list-style-type: none"> • What is Algebraic Thinking? Group 2 Presents Lesson Plans	Brahier: pp. 207- 216 (3 rd ed.) pp. 222-234 (4 th ed.)	
Nov 18	Considerations for Teaching Algebra (continued): Alternative Perspectives <ul style="list-style-type: none"> • Role of Representations • Functions Approach 	Selected readings - see course site	<i>Graduate students only</i> Collection of Activities Due (Upload to Blackboard) Lesson Plan #3 Due

Nov 25	Considerations for Teaching Algebra (continued) <ul style="list-style-type: none"> • Function Approach (cont.) • Algebra as a “Gatekeeper” • Algebra for All? Group 3 Presents Lesson Plans	Selected readings – see course site	Scheduled Design Conference
Dec 2	Considerations for Teaching Geometry <ul style="list-style-type: none"> • Importance of Spatial Reasoning • The van Hiele Model • Proof and argumentation 	Brahier: pp. 216 - 226 (3 rd ed.) pp. 237-248 (4 th ed.) Selected readings - See course site	All field work completed with accompanying assignments and log sheet (Bring to class or Upload to Blackboard) Lesson Plan #4 Due (Upload to Taskstream)
Dec 16	Lesson Plan Presentations and Revisiting our Mathematics Autobiographies <i>(Final Exam Day 7:30-10:15 p.m.)</i> All Students Present Final Lesson Plans		

Rubric for Performance Based Assessment: Lesson Plan Assignment

This rubric consists of 15 categories. Teacher candidates receive a score of 0, 1, 2, or 3 on each. In order to pass the assignment, teacher candidates must earn a minimum of “1” on all categories and a mean of at least “2” on the entire rubric. Candidates earning lower than a mean of “2” or a “0” on any category will be required to redo the assignment.

	Distinguished (met) 3	Proficient (met) 2	Developing (not met) 1	Unacceptable 0
Lesson Construction	Lesson and assignment are written in alignment with specified formatting. All accompanying materials/resources are included. Each resource is clear and appealing to students.	Lesson and assignment are written in alignment with specified formatting. All accompanying materials/resources are included. Some resources are not clear and/or appealing to students.	Lesson and assignment are written in alignment with specified formatting. Some materials are missing and/or all materials are unclear to students.	Lesson and assignment are not written in alignment with specified formatting and/or all submitted accompanying materials are not clear to students.
Goals/Objectives <i>InTASC: 7</i> <i>NCTM SPA: 8.4</i>	All goals and objectives are written to describe learning <u>outcomes</u> and are aligned with state and NCTM standards. None are extraneous.	Some objectives/goals are not written to describe learning <u>outcomes</u> . Most of the objectives/goals are related to standards. None are extraneous.	Objectives/goals are not written as learning <u>outcomes</u> . Some of the objectives/goals are related to standards. Some are extraneous.	Objectives/goals are missing, unclear, or are unrelated to standards. Some or all are extraneous.
Content <i>InTASC: 1</i>	Instruction focuses on the “big ideas” of mathematics and shows connections between and among concepts. Content is represented accurately and developed logically.	Instruction focuses on the “big ideas” of mathematics but some connections between and among concepts may be missing. Content is represented accurately but, at times, may have gaps in its logical development.	Instruction does not focus on the “big ideas” of mathematics and does not show connections between and among concepts. Content is, represented accurately but, at time, may have gaps in its logical development.	Instruction does not focus on the “big ideas” of mathematics and does not show connections between and among concepts. Content is not represented accurately and/or developed logically.
Student Learning <i>InTASC: 2</i> <i>NCTM SPA: 7.2, 7.4</i>	All planned activities are developmentally appropriate and provide opportunities for students to engage in meaningful exploration of mathematics in the development of conceptual understanding and procedural knowledge.	Most planned activities are developmentally appropriate and provide opportunities for students to engage in meaningful exploration of mathematics in the development of conceptual understanding and procedural knowledge.	Some planned activities are developmentally appropriate and provide opportunities for students to engage in meaningful exploration of mathematics in the development of conceptual understanding and procedural knowledge.	None of the planned activities are developmentally appropriate nor do they provide opportunities for students to engage in meaningful exploration of mathematics in the development of conceptual understanding and procedural knowledge.
Instructional Activities <i>InTASC: 4</i> <i>NCTM SPA: 7.2, 8.7</i>	Instruction regularly incorporates variety of activities, engages students in high-level thinking, is problem-/inquiry-based, and is creatively designed.	Instruction often incorporates a variety of activities, engages students in high-level thinking, is problem-/inquiry-based, and is creatively designed.	Instruction rarely incorporates a variety of activities, engages students in high-level thinking, is problem-/inquiry-based, and is creatively designed.	Instruction does not incorporate a variety of activities, engage students in high-level thinking, is not problem-/inquiry-based, and is not creatively designed.

Technology Integration <i>InTASC: 6</i> <i>NCTM SPA: 6, 7.6, 8.9</i>	Technology is appropriately integrated and supports the development of student understanding of mathematics.	Some technology is used; it has limited appropriateness for some learners and/or does not support the development of student understanding of mathematics.	Technology is not appropriately used; technology does not match goals of the lesson and/or does not support the development of student understanding of mathematics.	Technology is not evident in the lesson.
Communication <i>InTASC: 5, 6</i>	Instruction frequently provides opportunities for students to develop understandings collaboratively, in groups, as well as individually. Activities frequently encourage communication between and among students and teacher.	Instruction often provides opportunities for students to develop understandings collaboratively, in groups, as well as individually. Activities often encourage communication between and among students and teacher.	Instruction rarely provides opportunities for students to develop understandings collaboratively, in groups, as well as individually. Activities rarely encourage communication between and among students and teacher.	Instruction does not provide opportunities for students to develop understandings collaboratively, in groups, as well as individually. Activities do not encourage communication between and among students and teacher.
Professional Resources <i>InTASC: 10</i> <i>NCTM SPA: 8.5</i>	Lesson plans include at least one activity that is a modification of one found in a professional resource. Modifications and/or use in the lesson are well-designed to support student understanding of mathematics.	Lesson plans include at least one activity that is a modification of one found in a professional resource. Modifications and/or use in the lesson are not well-designed to support student understanding of mathematics.	Lesson plans include at least one activity that is a modification of one found in a professional resource. No attempt to modify was made.	Lesson plans do not include reference to outside source.
Justification for Instructional Decisions <i>InTASC: 9, 10</i> <i>NCTM SPA: 7.4, 8.6</i>	Instructional decisions are aligned with research-based recommendations. Narrative includes <i>meaningful</i> references to Brahier, NCTM, and additional readings for justification of instructional decisions. Narrative provides evidence of reflection on instruction designed to engage students in meaningful exploration of mathematical content that supports development of the NCTM process standards.	Instructional decisions are aligned with research-based recommendations. Narrative includes a few references to Brahier, NCTM, additional readings, and outside sources. Narrative provides evidence of reflection on instruction designed to engage students in meaningful exploration of mathematical content that supports development of the NCTM process standards	Instructional decisions are not aligned with research-based recommendations and/or narrative is weak with few references and/or little reflection on instruction designed to engage students in meaningful exploration of mathematical content that supports development of the NCTM process standards	Instructional decisions are not aligned with research-based recommendations. Narrative and reflection are weak and/or nonexistent.

Mathematical Problem Solving (ICTM SPA Standard 1)

Plans include opportunities for students to engage in the following:

- Apply and adapt a variety of appropriate strategies to solve problems
- Solve problems that arise in mathematics and those that arise in other contexts
- Build mathematical knowledge through problem solving
- Monitor and reflect on the process of problem solving

Distinguished (met) 3	Proficient (met) 2	Developing (not met) 1	Unacceptable 0
Lessons are designed as problem-based lessons. Throughout, students are consistently engaged in activities that address all 4 indicators.	Lessons are designed as problem-based lessons. Students are somewhat engaged in activities that address all 4 indicators.	Lessons are designed as problem-based lessons. Students are somewhat engaged in activities that address most of the indicators.	Lessons are not designed as problem-based lessons. Students are not engaged in activities that address most of the indicators.

Reasoning and Proof (ICTM SPA Standard 2)

Plans include opportunities for students to engage in the following:

- Develop a recognition of reasoning and proof as fundamental aspects of mathematics
- Make and investigate mathematical conjectures
- Develop and evaluation mathematical arguments and proofs
- Select and use various types of reasoning and methods of proof

Distinguished (met) 3	Proficient (met) 2	Developing (not met) 1	Unacceptable 0
Lessons are designed to engage students in reasoning and proof. Throughout, students are consistently engaged in activities that address all 4 indicators.	Lessons are designed to engage students in reasoning and proof. Students are somewhat engaged in activities that address all 4 indicators.	Lessons are designed to engage students in reasoning and proof. Students are somewhat engaged in activities that address most of the indicators.	Lessons are not designed to engage students in reasoning and proof. Students are not engaged in activities that address most of the indicators.

Mathematical Communication (ICTM SPA Standard 3)

Plans demonstrate and provide opportunities for students to engage in the following:

- Communicate their mathematical thinking coherently and clearly to peers, faculty, and others
- Use the language of mathematics to express ideas precisely
- Organize mathematical thinking through communication
- Analyze and evaluate the mathematical thinking and strategies of others

Distinguished (met) 3	Proficient (met) 2	Developing (not met) 1	Unacceptable 0
Lessons are designed to demonstrate skill in and engage students in mathematical communication. Throughout, students are consistently engaged in activities that address all 4 indicators.	Lessons are designed to demonstrate skill in and engage students in mathematical communication. Students are somewhat engaged in activities that address all 4 indicators.	Lessons are designed to demonstrate skill in and engage students in mathematical communication. Students are somewhat engaged in activities that address most of the indicators.	Lessons are not designed to demonstrate skill in and engage students in mathematical communication. Students are not engaged in activities that address most of the indicators.

Knowledge of Mathematical Connections (*ICTM SPA Standard 4*)

Plans demonstrate and provide opportunities for students to engage in the following: Recognize and use connections among mathematical ideas
 Recognize and apply mathematics in contexts outside of mathematics
 Demonstrate how mathematical ideas interconnect and build on one another

Distinguished (met) 3	Proficient (met) 2	Developing (not met) 1	Unacceptable 0
Lessons are designed to demonstrate and develop understanding of mathematical connections. Throughout, students are consistently engaged in activities that address all 3 indicators.	Lessons are designed to demonstrate and develop understanding of mathematical connections. Students are somewhat engaged in activities that address all 3 indicators.	Lessons are designed to demonstrate and develop understanding of mathematical connections. Students are somewhat engaged in activities that address most of the indicators.	Lessons are not designed to demonstrate and develop understanding of mathematical connections. Students are not engaged in activities that address most of the indicators.

Mathematical Representation (*ICTM SPA Standard 5*)

Plans demonstrate and provide opportunities for students to engage in the following:
 Use representations to model and interpret physical, social, and mathematical phenomena
 Create and use representations to organize, record, and communicate mathematical ideas
 Select, apply, and translate among mathematical representations to solve problems.

Distinguished (met) 3	Proficient (met) 2	Developing (not met) 1	Unacceptable 0
Lessons are designed to demonstrate and allow students to demonstrate knowledge of mathematical representations. Throughout, students are consistently engaged in activities that address all 3 indicators.	Lessons are designed to demonstrate and allow students to demonstrate knowledge of mathematical representations. Students are somewhat engaged in activities that address all 3 indicators.	Lessons are designed to demonstrate and allow students to demonstrate knowledge of mathematical representations. Students are somewhat engaged in activities that address most of the indicators.	Lessons are not designed to demonstrate and allow students to demonstrate knowledge of mathematical representations. Students are not engaged in activities that address most of the indicators.