# George Mason University College of Education and Human Development Mathematics Education Leadership

EDCI 644.6M5 – Mathematics Learning and Assessment (K-8) 3 Credits, Spring 2019
Wednesdays/7:20 p.m.-10:00 p.m. Online

**Faculty** 

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## **Prerequisites/Corequisites**

Admission to the Mathematics Education Leadership Master's degree program or instructor permission.

## **University Catalog Course Description**

Introduces students to learning theories and associated assessment practices specific to mathematics education. Intended for mathematics specialists and teachers interested in problems of learning and assessment across K-8 settings in mathematics education. This course is designed for master's level students in the mathematics education leadership program.

## **Course Overview**

Not Applicable.

## **Course Delivery Method**

This course will be delivered online (76% or more) using a synchronous format via Blackboard Learning Management system (LMS) housed in the MyMason portal. You will log in to the Blackboard (Bb) course site using your Mason email name (everything before @masonlive.gmu.edu) and email password. The course site will be available on January 28, 2019.

Under no circumstances, may candidates/students participate in online class sessions (either by phone or Internet) while operating motor vehicles. Further, as expected in a face-to-face class meeting, such online participation requires undivided attention to course content and communication.

## Technical Requirements

To participate in this course, students will need to satisfy the following technical requirements:

• High-speed Internet access with standard up-to-date browsers. To get a list of Blackboard's supported browsers see:

https://help.blackboard.com/Learn/Student/Getting Started/Browser Support#supported-browsers

To get a list of supported operation systems on different devices see:

https://help.blackboard.com/Learn/Student/Getting Started/Browser Support#tested-devices-and-operating-systems

- Students must maintain consistent and reliable access to their GMU email and Blackboard, as these are the official methods of communication for this course.
- Students will need a headset microphone for use with the Blackboard Collaborate web conferencing tool.
- Students may be asked to create logins and passwords on supplemental websites and/or to download trial software to their computer or tablet as part of course requirements.
- The following software plug-ins for PCs and Macs, respectively, are available for free download:
  - o Adobe Acrobat Reader: <a href="https://get.adobe.com/reader/">https://get.adobe.com/reader/</a>
  - o Windows Media Player:

https://support.microsoft.com/en-us/help/14209/get-windows-media-player

o Apple Quick Time Player: www.apple.com/quicktime/download/

## **Expectations**

- <u>Course Week:</u> Our course week will begin on the day that our synchronous meetings take place as indicated on the Schedule of Classes.
- <u>Log-in Frequency:</u>

Students must actively check the course Blackboard site and their GMU email for communications from the instructor, class discussions, and/or access to course materials at least 3 times per week. In addition, students must log-in for all scheduled online synchronous meetings.

• <u>Participation:</u>

Students are expected to actively engage in all course activities throughout the semester, which includes viewing all course materials, completing course activities and assignments, and participating in course discussions and group interactions.

• Technical Competence:

Students are expected to demonstrate competence in the use of all course technology. Students who are struggling with technical components of the course are expected to seek assistance from the instructor and/or College or University technical services.

• Technical Issues:

Students should anticipate some technical difficulties during the semester and should, therefore, budget their time accordingly. Late work will not be accepted based on individual technical issues.

## • Workload:

Please be aware that this course is **not** self-paced. Students are expected to meet *specific deadlines* and *due dates* listed in the **Class Schedule** section of this syllabus. It is the student's responsibility to keep track of the weekly course schedule of topics, readings, activities and assignments due.

## • Instructor Support:

Students may schedule a one-on-one meeting to discuss course requirements, content or other course-related issues. Those unable to come to a Mason campus can meet with the instructor via telephone or web conference. Students should email the instructor to schedule a one-on-one session, including their preferred meeting method and suggested dates/times.

## • Netiquette:

The course environment is a collaborative space. Experience shows that even an innocent remark typed in the online environment can be misconstrued. Students must always re-read their responses carefully before posting them, so as others do not consider them as personal offenses. *Be positive in your approach with others and diplomatic in selecting your words*. Remember that you are not competing with classmates, but sharing information and learning from others. All faculty are similarly expected to be respectful in all communications.

## • Accommodations:

Online learners who require effective accommodations to insure accessibility must be registered with George Mason University Disability Services.

## **Learner Outcomes or Objectives**

This course is designed to enable students to do the following:

- 1. Understand the learning theories fundamental to mathematics education.
- 2. Understand the developmental progressions underpinning mathematics learning.
- 3. Develop an understanding of various forms of mathematics learning assessment related to theories of mathematics learning.
- 4. Understand the assessment of students' thinking at multiple levels.

## **Professional Standards (National Council of Teachers of Mathematics (NCTM))**

Upon completion of this course, students will have met the following professional standards:

## A. **Standard 4:** Mathematical Learning Environment

Effective elementary mathematics specialists exhibit knowledge of child, pre-adolescent, and adult learning, development, and behavior. They use this knowledge to plan, create, and assist teachers in planning and creating sequential learning opportunities grounded in mathematics education research where students are actively engaged in the mathematics they are learning and building from prior knowledge and skills. They demonstrate, promote, and assist teachers in demonstrating and promoting a positive disposition toward mathematical practices and learning and exhibit and support the equitable and ethical treatment of and

high expectations for all students. They include and assist teachers in embracing culturally relevant perspectives in teaching, in recognizing individual student differences, and in using instructional tools such as manipulatives, digital tools, and virtual resources to enhance student learning, while recognizing the possible limitations of such tools.

- **b.** Plan, create, and coach/mentor teachers in creating developmentally appropriate, sequential, and challenging learning opportunities grounded in mathematics education research in which students are actively engaged in building new knowledge from prior knowledge and experiences
- **d.** Demonstrate and encourage equitable and ethical treatment of and high expectations for all students.
- e. Apply mathematical content and pedagogical knowledge in the selection, use, and promotion of instructional tools such as manipulatives and physical models, drawings, virtual environments, presentation tools, and mathematics-specific technologies (e.g., graphing tools and interactive geometry software); and make and nurture sound decisions about when such tools enhance teaching and learning, recognizing both the insights to be gained and possible limitations of such tools

## **Required Texts**

Donovan, M. S. & Bransford, J. (2004). *How students learn: Mathematics in the classroom.* Washington D.C., National Research Council.

FREE PDF: https://www.nap.edu/catalog/11101/how-students-learn-mathematics-in-the-classroom

Fennell, F., Kobett, B. M., & Wray, J. A. (2017). *The formative 5: Everyday assessment techniques for every math classroom.* Thousand Oaks, CA: Corwin.

Silver, E. A., & Mills, V. L. (Eds.). (2018). *A fresh look at formative assessment in mathematics teaching*. Reston, VA: NCTM

## **Course Performance Evaluation**

Students are expected to submit all assignments on time in the manner outlined by the instructor (e.g., Blackboard, Tk20, hard copy).

This course will introduce students to the diverse learning theories and associated assessment practices specific to mathematics education. Topics will also include the historical development of learning theories as well as emerging theories. Assessment topics will include test design, problem-based assessment as well as other forms of assessment of mathematics learning across K-8. The course is intended for mathematics specialists, mathematics teachers, and pre-service mathematics teachers interested in problems of learning and assessment in mathematics education.

Additional details and rubrics for all assignments will be posted on Blackboard. Please review

## these materials.

## • Assignments and/or Examinations

## Participation (10%)

The quality of this course depends heavily and primarily on the regular attendance and participation of all involved. Participation will include taking part in discussions informed by critical reading and thinking and sharing with the class the products of various reading/writing assignments and teacher leader experiences.

	LEVEL OF PERFORMANCE				
ELEMENT	Distinguished	Proficient	Basic	Unsatisfactory	
	(9 – 10 points)	(8 points)	(6 - 7 points)	(1 - 5 points)	
Attendance & Participatio n	The student attends all classes, is on time, is prepared and follows outlined procedures in case of absence.  The student actively participates and continually supports the members of the learning group and the members of the class, including online Discussion Boards, when applicable.  Presentations demonstrate a deep knowledge of content as well as implications for teaching.	The student attends all classes, is on time, is prepared and follows outlined procedures in case of absence.  The student makes active contributions to the learning group and class, including online Discussion Boards, when applicable.  Presentations demonstrate sufficient knowledge of content as well as implications for teaching.	The student misses 1 or 2 classes and follows outlined procedures in case of absence. At times the student is not prepared for class.  The student is on time, prepared for class, and participates in group and class discussions, including online Discussion Boards, when applicable.  Presentations demonstrate minimal knowledge of content and/or implications for teaching.	The student is frequently late for class or absences are not documented by following the outlined procedures.  The student is frequently not prepared for class and does not actively participate in discussions, including online Discussion Boards, when applicable.  Presentations are lacking knowledge of content and connections to teaching.	

## **Mathematics Assessment Autobiography (5%)**

How you teach is inseparable from what you believe about mathematics, learning, and teaching. This assignment is intended to bring to light your educational and other personal experiences that influence your expectations and understanding of mathematics, teaching and learning. You will reflect upon your own beliefs and actions in regards to teaching and learning mathematics, as well as think about how you might encourage others on the topic of mathematical data and assessments. You will also self-assess your learning directed by this

assignment. The specific guiding questions for reflection and self-assessment can be found in your Blackboard Course site.

## Online Assessment Tool Analysis Video (25%)

Students will prepare a short video that explains and summarizes a particular type of online mathematics assessment (e.g., formative, summative, portfolios, multiple-choice, warm-ups) that could be used with teachers. Learning how to effectively and efficiently prepare materials for teachers is an ability mathematics specialists need to develop and to refine. The goal is for you to learn about the type of assessment and to learn how to disseminate information to adult learners.

## **Group Mathematics Topics and Learning Progression Project (25%)**

In groups, the students will explore research literature on their topic, create an annotated bibliography of the literature, select an article that could be shared with teachers, prepare an appropriate assessment within the topic, and prepare a handout on the topic for their peers. Students will explore and present information on one of the following topics and how they address learning progressions for students:

- Presentations in Class 6
  - o K-2 Rational Numbers
- Presentations in Class 7
  - o 3-5 Rational Numbers
  - o 3-8 Rational Numbers
- Presentations in Class 8
  - o 6-8 Rational Numbers

## Clinical Interview (30%)

Effective teaching requires a keen awareness of how and what your students are thinking and understanding. The experience of conducting a clinical interview is intended to increase your awareness of students' thinking and learning in a detailed manner about a particular mathematics topic. The other focus of this assignment is on concrete manipulatives and their relationship to learning. So, you should select a manipulative (or manipulatives) to accompany the task and then assess how well the manipulative helped the learner to solve the problem. This is your Performance Based Assessment for this course. See the project description and rubric which follow the course schedule.

## Final Reflection (5%)

This assignment is intended for you to reflect upon the knowledge you have gained this semester and how it is informing your beliefs and practices. You will reflect upon your own beliefs and actions in regards to teaching and learning mathematics, as well as think about how you might encourage others on the topic of mathematical data and assessments. You will also self-assess your learning directed by this assignment. The specific guiding questions for reflection and self-assessment can be found in your Blackboard Course site.

## • Other Requirements

## **APA Formatting**

All assignments require APA formatting:

American Psychological Association (2010). *Publication Manual of the American Psychological Association*. American Psychological Association: Washington, DC.

#### Attendance

It is your responsibility to attend all class sessions. You are held accountable for all information from each class session whether you are present or not. Reasons for any absence must be reported to the instructor in writing.

#### **Tardiness**

It is your responsibility to be on time for each class session. Please report your reasons for any tardiness to the instructor in writing. Class materials will be posted for each class session on Blackboard. Students are responsible for reviewing these materials and submitting required artifacts (where appropriate) to online class discussion boards.

## **Course Performance Evaluation Weighting**

10%	Participation
5%	Mathematical Assessment Autobiography
25%	Online Assessment Tool Analysis Video
25%	Group Mathematics Topics and Learning Progressions Project
30%	Clinical Interview
5%	Final Reflection

## **Grading**

All assignments are to be turned in to your instructor on time. **Late work will not be accepted for full credit.** Assignments turned in late will receive a 10% deduction from the grade per late day or any fraction thereof (including weekends and holidays).

## The final evaluation criteria utilizes the graduate grading scale and is as follows:

A	93%-100%	$\mathrm{B}+$	87%-89%	С	70%-79%
A-	90%-92%	В	80%-86%	F	Below 70%

## • For Master's Degrees:

Candidates must have a minimum GPA of 3.00 in coursework presented on the degree application, which may include no more than 6 credits of C. (Grades of C+, C-, or D do not apply to graduate courses. The GPA calculation excludes all transfer courses and Mason non-degree studies credits not formally approved for the degree).

## • For Endorsement Requirements

Candidates must have a grade of B or higher for all licensure coursework (endorsement coursework).

## **Professional Dispositions**

Students are expected to exhibit professional behaviors and dispositions at all times. Education professionals are held to high standards, both inside and outside of the classroom. Educators are evaluated on their behaviors and interactions with students, parents, other professionals, and the community at large. At the College of Education and Human Development, dispositions may play a part in the discussions and assignments of any/all courses in a student's program (and thus, as part or all of the grade for those assignments). For additional information visit <a href="https://cehd.gmu.edu/students/polices-procedures/">https://cehd.gmu.edu/students/polices-procedures/</a>

## **Class Schedule**

HSL = How Students Learn F5 = Formative 5 AFLFA = A Fresh Look on Formative Assessment

Date	Topics	Readings Due	Assignments Due
Week 1	Technology Briefing		Create Collaborate Profile
1/28	Class Overview		(Including Picture)
	Introduction		
Format	Assessment Reflection		
Synchronous	Interviews		
Week 2	Principles of Learning	HSL: Ch. 1	Mathematics Assessment
2/4	Theories & Mathematical	F5: Part 1	Autobiography
	Understanding	AFLAFA: Foreword & Preface	
Format			
Synchronous			
Week 3	Observations	HSL: Ch. 5	
2/11		F5: Chapter 1	
	Formative Assessment:	AFLAFA: Chapter 1 & 2	
Format	What, Why & How?		
Synchronous			
	Library Tools for		
	Research: Anne Driscoll		
	Presentation		
Week 4	Interviews	F5: Chapter 2	
2/18		AFLAFA: Chapter 3 & 4	
	Designing A Clinical	Fernandez (2009)	
Format	Interview		
Synchronous			
	Classroom Discourse		
	Cognitively Guided		
	Instruction		
	ELLs		
Week 5	Show Me	F5: Chapter 3	
2/25		AFLAFA: Chapter 5 & 6	
	Culturally Responsive		
Format	Pedagogy		
Synchronous			
	Learning Trajectories		
	11.		
Week 6	Hinge Questions	F5: Chapter 4	

3/4		AFLAFA: Chapters 7 & 8	
	Mathematical Tasks	-	
Format			
Synchronous	Response to Intervention		
Week 7	Whole Number Sense	HSL: Chapter 6	Group 1 & 2 Presentations
3/11	Learning Progressions	1	
			Clinical Interview: Protocol
GMU Spring Break			Draft Due
Format Synchronous			
Week 8	Rational Number System	HSL: Chapter 7	Group 3 & 4 Presentations
3/18	Learning Progressions		Group 1 & 2 Mathematics
			Topics and Learning
Format			Progressions Project Due
Synchronous			
Week 9	Functions Learning	HSL: Chapter 8 Section	Group 5 & 6 Presentations
3/25	Progressions	TISE. Chapter o Section	Group 5 & 0 1 resentations
			Group 3 & 4 Mathematics
Format			Topics and Learning
Synchronous			Progressions Project Due
Week 10	Video Assessment Tool		Online Assessment Tool
4/1	Work Session		Analysis Video Due
Format	Clinical Interview Work		Group 5 & 6 Mathematics
Asynchronous	Session: Clinical		Topics and Learning
	Interview Part II		Progressions Project Due
Week 11	Video Assessment Tool		
4/8	Reflection		
Format	Clinical Interview Work		
Asynchronous	Session: Clinical Interview Part II		
	miciview Part II		
4/15		No Class Meeting	
Week 12	Improving Mathematics	AFLAFA: Chapters 9 & 10	
W CCR 12	improving maniemanes	711 D. 11 71. Chapters 7 & 10	

4/22	Instruction		
Format Synchronous	Equitable Mathematics Classrooms		
Week 13	A Vision	AFLAFA: Chapters 11 & 12	
4/29  Format  Synchronous	Moving Forward	NCTM Position Statement (2016): Large-Scale Assessments	
		NCSM & AMTE Position Statement (2013): Improving Student Achievement in Mathematics Through Formative Assessment in Instruction	
Week 14	Clinical Interview Work		
5/6	Session: Part III		
Format Asynchronous	Final Reflection (Optional)		
Week 15 5/13		Sharing of Clinical Interview Projects	Clinical Interview Due
Format Synchronous		Final Reflection (Time in Class)	

Note: Faculty reserves the right to alter the schedule as necessary, with notification to students.

## **Core Values Commitment**

The College of Education and Human Development is committed to collaboration, ethical leadership, innovation, research-based practice, and social justice. Students are expected to adhere to these principles: <a href="http://cehd.gmu.edu/values/">http://cehd.gmu.edu/values/</a>.

## **GMU Policies and Resources for Students**

## **Policies**

• Students must adhere to the guidelines of the Mason Honor Code (see <a href="https://catalog.gmu.edu/policies/honor-code-system/">https://catalog.gmu.edu/policies/honor-code-system/</a>).

- Students must follow the university policy for Responsible Use of Computing (see <a href="http://universitypolicy.gmu.edu/policies/responsible-use-of-computing/">http://universitypolicy.gmu.edu/policies/responsible-use-of-computing/</a>).
- Students are responsible for the content of university communications sent to their Mason email account and are required to activate their account and check it regularly. All communication from the university, college, school, and program will be sent to students solely through their Mason email account.
- Students with disabilities who seek accommodations in a course must be registered with George Mason University Disability Services. Approved accommodations will begin at the time the written letter from Disability Services is received by the instructor (see <a href="https://ds.gmu.edu/">https://ds.gmu.edu/</a>).
- Students must silence all sound emitting devices during class unless otherwise authorized by the instructor.

## Campus Resources

- Support for submission of assignments to Tk20 should be directed to <a href="mailto:tk20help@gmu.edu">tk20help@gmu.edu</a> or <a href="https://cehd.gmu.edu/aero/tk20">https://cehd.gmu.edu/aero/tk20</a>. Questions or concerns regarding use of Blackboard should be directed to <a href="https://coursessupport.gmu.edu/">https://coursessupport.gmu.edu/</a>.
- For information on student support resources on campus, see <a href="https://ctfe.gmu.edu/teaching/student-support-resources-on-campus">https://ctfe.gmu.edu/teaching/student-support-resources-on-campus</a>

For additional information on the College of Education and Human Development, please visit our website <a href="https://cehd.gmu.edu/students/">https://cehd.gmu.edu/students/</a>.

## **EDCI 644 - Expectations Clinical Interview Assessment** (30% of Grade) **Performance- Based Assessment**

#### NCTM Standards 4b, 4d, 4e

#### PART I: The Plan

## Student Description:

- Describe the student you plan to assess
  - o Include information you gathered about the child (grade level, age, gender, race, and academic ability level)
  - What do you know about the child's level of understanding about the topic before the assessment?

#### The Mathematics Concept Development & Learning Progression:

- Select one specific mathematics concept to assess during the assessment.
  - Examples of concepts might include patterns, sorting, addition of whole numbers, division
    of fractions, finding averages, percent, geometric shapes, or length measurement. Tell why
    this concept is appropriate for this child at this particular grade level.

## **Different Forms of Representation:**

- During the assessment, assess the child using three different forms of representation.
- Identify the three different forms of representation you will use during the assessment with at least one example in each form.
  - o *Concrete* representations include manipulatives, measuring tools, or other objects the child can manipulate during the assessment.
  - o *Pictorial* representations include drawings, diagrams, charts, or graphs that are drawn by the child or are provided for the child to read and interpret.
  - Symbolic representations include numbers or letters the child writes or interprets to demonstrate understanding of a task.

#### Tasks & Questions:

- Design tasks and questions that use three different forms of representation (concrete, pictorial, symbolic) to diagnose the child's understanding of ONE basic concept. The goal is to assess students' conceptual understanding, procedural fluency, strategic competence, adaptive reasoning and productive dispositions towards mathematics.
- Go beyond the basic level of determining the child's factual knowledge of the concept by asking questions that determine how much the child understands about the concept.
  - o For example, suppose you are assessing the concept of ADDITION.
  - Create several tasks where the child uses concrete manipulatives to demonstrate his or her understanding of addition; ask questions about the child's understanding of the addition tasks with manipulatives.
  - Create several tasks where the child is asked to create or interpret drawings to demonstrate her understanding of addition; ask questions about the child's understanding of these tasks with pictorial models
  - Create several tasks where the child uses abstract symbols (and letters) to demonstrate her understanding of addition; ask questions about the child's understanding of these addition tasks using the symbols.

#### **PART II: Analysis of Evidence**

#### **Student Work Samples:**

• Collect and document three different forms of representation (concrete, pictorial, symbolic) during the assessment to elicit the child's level of understanding. The report must include samples of the child's computations, writings and drawings, as well as a description of how the child used concrete objects during the assessment or photographs of the child's work.

#### Question & Response Assessment Segments

- Audiotape the assessment.
- For the report, choose segments of your questions and the child's responses. Indicate what you said and what the child said.

#### Questioning Competence:

The questions and follow-up questions that you use during the assessment will be evaluated. You
will be evaluated on the <u>quality</u> and the <u>types</u> of follow-up questions you use during your
interaction with the child. Your textbooks and readings provide direction on the types of questions
that are appropriate in an assessment and that go beyond factual information to deeper
understanding.

## **PART III: Evaluation and Instructional Implications**

## Evaluation of Child's Mathematical Knowledge:

- Write an evaluation of the child's mathematical knowledge in the content area.
- Use evidence from the assessment to support your conclusions.
- Use your textbook to help you describe the specific types of behaviors and verbalizations you observed using specific mathematical terms. For example, if you conclude that the student has an understanding of addition of fractions with like denominators, you should base this on evidence that you present that shows the child was able to represent 3/5 and 4/5 with fraction pieces (concrete), and/or the child used a drawing to find the sum (pictorial), and/or the child computed the answer with symbols (abstract).
- Give specific examples of the child's responses to support your statements.

#### Instructional Plan:

- Develop a suggested instructional plan for the child.
  - Your assessment of the child's thinking should give you some information for planning instruction. Your suggestions should be based on what you learned about the child during the assessment. Many general suggestions can be valuable for children. However, your recommendations should relate to specifics. For example, if you assessed basic division concepts and you suggest that the instructional plan for the child should include more manipulatives, that would be an important teaching strategy, but it would be too general. You should be more specific about why and how manipulatives might be used. Example: "The student had difficulty making 3 equal groups from a set of 21 chips; therefore, the student should be given more experiences with grouping and partitioning manipulatives in sets of 15 to 30 to develop both the measurement and partitive concepts of division."

#### **Part IV: Reflection**

## Reflection of the Assessment Process

- Comment on the assessment process.
  - How long did the assessment last?What did you learn about assessment techniques?
  - What did you learn about your ability to create mathematics questions and tasks for this concept?
  - o If you were to conduct the assessment with another child, would there be any changes in your questions, either the order or the level of difficulty, or the materials you had available for the child to use? Why or why not?
  - What have you learned about how children learn mathematics from this assessment? How might a classroom teacher use the diagnostic mathematics assessment to assess children?

Clinical Interview Rubric (Course Performance-Based Assessment)				
Level/Criteria	4	3	2	1
	Exceeds	Meets	Developing	Does Not Meet
	Expectations	Expectations		Expectations
CLINICAL INTERVIEW PA				
THE CHILD	The plan includes a	The plan includes a	The plan includes a	The plan includes a
NCTM Standard 4d	positive description	positive description of the child with all	positive description	positive description
Demonstrate and	of the child with all of the following	of the following	of the child with five of the	of the child with fewer than five of
encourage equitable	elements:	elements:	following elements:	the following
and ethical treatment	cicinents.	ciements.	Tollowing cicinches.	elements:
of and high	• Grade level	Grade level	Grade level	
expectations for all	●Age	● Age	● Age	<ul> <li>● Grade level</li> </ul>
students.	• Gender	• Gender	• Gender	● Age
	• Race	• Race	• Race	● Gender
	Academic ability	Academic ability	Academic ability	• Race
	level	level	level	<ul> <li>Academic ability</li> </ul>
	• Child's	● Child's	● Child's	level
	mathematical	mathematical	mathematical	● Child's
				mathematical
	understanding on	understanding on	understanding on	understanding on
	the mathematics	the mathematics	the mathematics	the mathematics
	topic assessed	topic assessed	topic assessed	
	● Child's			topic assessed
	performance in			
	other academic			
	areas			
	● Child's			
	performance in			
	social or			
	behavioral areas			
THE MATHEMATICS	The plan describes	The plan describes	The plan describes	The plan does not
THE MATHEMATICS CONCEPT & FORMS	the mathematics	the mathematics	the mathematics	The plan does not describe the
OF REPRESENTATION	concept and forms	concept and forms	concept and forms	mathematics
	of representation	of representation	of representation	concept and forms
NCTM Standard 4e	with all of the	with all of the	with all of the	of representation
Apply mathematical	following elements:	following elements:	following elements:	or is missing one of
content and				following elements:
pedagogical	<ul><li>Information on</li></ul>	<ul><li>Information on</li></ul>	<ul><li>Information on</li></ul>	
knowledge in the	age-appropriate	age-appropriate	age-appropriate	• Information on
selection, use, and promotion of	variations of the	variations of the	variations of the	age-appropriate
instruction of	mathematics	mathematics	mathematics	variations of the
such as manipulatives	concept	concept	concept	mathematics
and physical models,	● One clearly-	● One clearly-	● One clearly-	concept
drawings, virtual	described and	described and	described and	● One clearly-
environments,	mathematically-	mathematically-	mathematically-	described and
presentation tools,				mathematically-

and mathematics-	accurate.	accurate.	accurate.	accurate.
specific technologies (e.g., graphing tools	concept	concept	concept	concept
and interactive	<ul><li>◆Three different</li></ul>	<ul><li>Three different</li></ul>	<ul><li>Three different</li></ul>	<ul><li>Three different</li></ul>
geometry software)	forms of	forms of	forms of	forms of
geometry continue,	representation,	representation,	representation,	representation,
	with different	with different	with different	with different
	examples in each	examples in each	examples in each	examples in each
	form, are	form, are	form, are	form, are
	designed for use	designed for use	designed for use	designed for use
	in interesting and	in interesting and	in interesting and	in interesting and
	creative ways	creative ways	creative ways	creative ways
	• Connections	● Connections	,	,
	among	among		
	representational	representational		
	forms	forms		
	References are	1011113		
	cited.			
TASKS & QUESTIONS	The plan describes	The plan describes	The plan describes	The plan describes
NCTM Standard 4e	tasks and questions	tasks and questions	tasks and questions	tasks and questions
	with all of the	with all of the	with three of the	with two or fewer
Apply mathematical	following elements:	following elements:	following elements:	of the following
content and				elements:
pedagogical	• Tasks and	• Tasks and	• Tasks and	● Tasks and
knowledge in the selection, use, and	questions are	questions are	questions are	
promotion of	aligned with the	aligned with the	aligned with the	questions are
instructional tools	math concept.	math concept.	math concept.	aligned with the
such as manipulatives	<ul><li>Questions allow</li></ul>	<ul> <li>Questions allow</li> </ul>	<ul> <li>Questions allow</li> </ul>	math concept.
and physical models,	for differentiation	for differentiation	for differentiation	<ul> <li>Questions allow</li> </ul>
drawings, virtual	and extensions	and extensions	and extensions	for differentiation
environments,	for different	for different	for different	and extensions
presentation tools,	levels of student	levels of student	levels of student	for different
and mathematics-	performance.	performance.	performance.	levels of student
specific technologies (e.g., graphing tools	<ul> <li>A variety of tasks</li> </ul>	<ul> <li>A variety of tasks</li> </ul>	<ul> <li>A variety of tasks</li> </ul>	performance.
and interactive	and questions for	and questions for	and questions for	<ul> <li>A variety of tasks</li> </ul>
geometry software)	each of the three	each of the three	each of the three	and questions for
	forms of	forms of	forms of	each of the three
	representation	representation	representation	forms of
	• Tasks show	● Tasks show	• Tasks show	representation
	creativity and will	creativity and will	creativity and will	<ul><li>Tasks show</li></ul>
	be motivating for	be motivating for	be motivating for	creativity and will
	a child.	a child.	a child.	be motivating for
	References are	<del></del>	<del>-</del>	a child.
	cited.			
CLINICAL INTERVIEW PA		-		
STUDENT WORK	The description of	The description of	The description of	The description of
SAMPLES	the student's	the student's	the student's	the student's
NCTM Element 4e	performance includes all of the	performance includes two of the	performance includes one of the	performance is
Apply mathematical				missing or includes none of the
Apply maniematical	following:	following:	following:	ווטוופ טו נוופ

content and				following:
pedagogical knowledge in the selection, use, and promotion of instructional tools such as manipulatives and physical models, drawings, virtual environments, presentation tools, and mathematics- specific technologies (e.g., graphing tools and interactive geometry software)	<ul> <li>A variety of work samples from the child showing examples in each of the three forms of representation (concrete, pictorial, and abstract)</li> <li>An explanatory analysis and overview of each of the child's work samples</li> <li>Clearly explained connections between student work samples.</li> </ul>	<ul> <li>A variety of work samples from the child showing examples in each of the three forms of representation (concrete, pictorial, and abstract)</li> <li>An explanatory analysis and overview of each of the child's work samples</li> <li>Clearly explained connections between student work samples</li> </ul>	<ul> <li>A variety of work samples from the child showing examples in each of the three forms of representation (concrete, pictorial, and abstract)</li> <li>An explanatory analysis and overview of each of the child's work samples</li> <li>Clearly explained connections between student work samples</li> </ul>	<ul> <li>A variety of work samples from the child showing examples in each of the three forms of representation (concrete, pictorial, and abstract)</li> <li>An explanatory analysis and overview of each of the child's work samples</li> <li>Clearly explained connections between student work samples</li> </ul>
TRANSCRIPT	The transcript	The transcript	The transcript	Transcript evidence
EVIDENCE	evidence includes:	evidence includes:	evidence includes:	is not provided.
Apply mathematical content and pedagogical knowledge in the selection, use, and promotion of instructional tools such as manipulatives and physical models, drawings, virtual environments, presentation tools, and mathematics-specific technologies (e.g., graphing tools and interactive geometry software)	• Several excerpts from the mathematics assessment using the teacher and the child's actual verbalizations from the assessment (T for teacher; C for child) • Descriptive information on the behaviors and verbalizations that occurred during the assessment	• Several excerpts from the mathematics assessment using the teacher and the child's actual verbalizations from the assessment (T for teacher; C for child)	• Few excerpts from the mathematics assessment using the teacher and the child's actual verbalizations from the assessment (T for teacher; C for child)	
EVIDENCE OF QUESTIONING NCTM Standard 4e	Questioning evidence includes all of the following:	Questioning evidence includes two of the following:	Questioning evidence includes one of the following:	Questioning evidence does not include the following:
Apply mathematical content and pedagogical	• A variety of questions	• A variety of	• A variety of	• A variety of

knowledge in the selection, use, and promotion of instructional tools such as manipulatives and physical models, drawings, virtual environments, presentation tools, and mathematics-specific technologies (e.g., graphing tools and interactive geometry software)

- encouraging the child to express his/her thinking
- Many higher-level questions to encourage deeper thinking and responses from the child
- Specific follow-up questions to probe for understanding
- questions
  encouraging the
  child to express
  his/her thinking
- Many higher-level questions to encourage deeper thinking and responses
- from the child
   Specific follow-up
  questions to
  probe for
  understanding
- questions encouraging the child to express his/her thinking
- Many higher-level questions to encourage deeper thinking and responses from the child
- Specific follow-up questions to probe for understanding

- questions encouraging the child to express his/her thinking
- Many higher-level questions to encourage deeper thinking and responses from the child
- Specific follow-up questions to probe for understanding

#### **CLINICAL INTERVIEW PART III: EVALUATION & INSTRUCTIONAL IMPLICATIONS**

#### THE EVALUATION

#### **NCTM Element 4b**

Plan, create, and coach/mentor teachers in creating developmentally appropriate, sequential, and challenging learning opportunities grounded in mathematics education research in which students are actively engaged in building new knowledge from prior knowledge and experiences.

- The evaluation of the child's understanding includes all of the following:
- An accurate and detailed description of the child's current level of understanding of the mathematics concept
- Many different and specific examples from the assessment are given to provide supporting evidence for the evaluation of the child (including the child's quotations and student work)
   Information from
- Information from other sources on mathematics development.

- The evaluation of the child's understanding includes two of the following:
- An accurate and detailed description of the child's current level of understanding of the mathematics concept
- Many different and specific examples from the assessment are given to provide supporting evidence for the evaluation of the child (including the child's quotations and student work)
- Information from other sources on mathematics development.

The instructional

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- An evaluation of the child's understanding includes one of the following:
- An accurate and detailed description of the child's current level of understanding of the mathematics concept
- Many different and specific examples from the assessment are given to provide supporting evidence for the evaluation of the child (including the child's quotations and student work)
   Information from other sources on

mathematics

development.

The instructional

- An evaluation of the child's understanding does not include the following:
- An accurate and detailed description of the child's current level of the mathematics concept
   Many different
- and specific examples from the assessment are given to provide supporting evidence for the evaluation of the child (including the child's quotations and student work) Information from other sources on mathematics development.

The instructional

## THE INSTRUCTIONAL

#### PLAN

#### **NCTM Element 4b**

Plan, create, and coach/mentor teachers in creating developmentally appropriate, sequential, and challenging learning opportunities grounded in mathematics education research in which students are actively engaged in building new knowledge from prior knowledge and experiences.

plan includes all of the following:

- A creative, detailed description of developmentally appropriate next steps for instruction taking into account the child's current level of understanding.
- Many specific examples of activities and tasks that would further enhance this child's knowledge of this math concept.
- Information from other sources on mathematics and development and child development are used in making the plan.
- References are cited.

plan includes all of the following:

- A creative, detailed description of developmentally appropriate next steps for instruction taking into account the child's current level of understanding.
- Many specific examples of activities and tasks that would further enhance this child's knowledge of this math concept.
   Information from
- Information from other sources on mathematics and development and child development are used in making the plan.

plan includes two of the following:

- A creative, detailed description of developmentally appropriate next steps for instruction taking into account the child's current level of understanding.
- Many specific examples of activities and tasks that would further enhance this child's knowledge of this math concept.
   Information from
- Information from other sources on mathematics and development and child development are used in making the plan.

plan includes one or none of the following:

- A creative, detailed description of developmentally appropriate next steps for instruction taking into account the child's current level of understanding.
- Many specific examples of activities and tasks that would further enhance this child's knowledge of this math concept.
- Information from other sources on mathematics and development and child development are used in making the plan.

#### **CLINICAL INTERVIEW PART IV: REFLECTION**

The reflection includes all of the following:

- Implementing the assessment
- Describing the clinical interview
- Learning about assessment techniques
- Creating questions and tasks for the mathematics

The reflection includes at least six of the following:

- Implementing the assessment
- Describing the clinical interview
- Learning about assessment techniques
- Creating questions and tasks for the mathematics

The reflection includes five of the following:

- Implementing the assessment
- Describing the clinical interview
- Learning about assessment techniques
- Creating questions and tasks for the mathematics

A reflection is provided that includes four or fewer of the following:

- Implementing the assessment
- Describing the clinical interview
- Learning about assessment techniques
- Creating questions and

concept	concept	concept	tasks for the
<ul><li>Adapting the</li></ul>	<ul><li>Adapting the</li></ul>	<ul><li>Adapting the</li></ul>	mathematics
interview for	interview for	interview for	concept
another child	another child	another child	<ul><li>Adapting the</li></ul>
<ul><li>Learning about</li></ul>	<ul> <li>Learning about</li> </ul>	<ul><li>Learning about</li></ul>	interview for
how children	how children	how children	another child
learn	learn	learn	<ul><li>Learning about</li></ul>
mathematics	mathematics	mathematics	how children
<ul><li>Describing how a</li></ul>	Describing how a	Describing how a	learn
classroom	classroom	classroom	mathematics
teacher might use	teacher might use	teacher might use	Describing how a
a diagnostic	a diagnostic	a diagnostic	classroom
mathematics	mathematics	mathematics	teacher might use
assessment	assessment	assessment	a diagnostic
			mathematics
			assessment